# Statistics & Probablities

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# What is Statistics ?

The science of making decisions and knowing statistics can help you make better decisions through out life

- 1. Collecting Data
- 2. Analyzing Data
- 3. Interpreting Data
- 4. Presenting Data

# Answer in 5 seconds

A college in US has students from the following countries. Which country is in majority ?

US	China	US	Sweden	China
Canada	China	Japan	Mexico	US
China	Germany	India	India	Japan
US	US	US Chir		China
India	Japan	England	India	Japan
England	India	China	Mexico	US
Mexico	US	Canada	Pakistan	India
Japan	China	US	Japan	Germany
China	India	India	China	China
Germany	Japan	China	US	Japan

### **Frequency** Table

#### **Properties of RF**

1. The range of proportions is between 0 and 1

2. Sum of relative frequencies =1

Country	Frequency
Canada	2
China.	12
England	2
Germany	3
India.	8
Japan	8
Mexico	3
Pakistan	1
Sweden	1
US	10

# Case Study

#### Problem

A parent changes school of their Son who is studying in 11<sup>th</sup> standard since his academic results are not good in the current School. They change Student A from **ABC school to XYZ school** 

#### Results

- 1. Ranked 15<sup>th</sup> in ABC school
- 2. Ranked 2<sup>nd</sup> in XYZ school

What's the conclusion: Has the student improved ?

### Number of Students

#### No of Students in ABC School



#### No of Students in XYZ School



# What's the most common Age ?

Students Age's

			-	
15	19	18	14	13
27	16	65	15	31
22	15	24	22	51
24	20	45	22	33
24	27	18	66	15
18	39	10	30	13
19	28	53	28	65
30	20	21	20	18
20	23	18	41	52
75	19	63	14	18

# Converting Data to Range – Histogram plot

Age	Frequency
0-19	19
20-39	21
40-59	5
60-79	5





Presenting, organizing and summarizing data

Classification

Drawing conclusions about a population based on data observed in a sample

### **Population and Sample**



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### **Census and Survey**

**Census:** Gathering data from the whole **population** of interest. For example, elections, 10-year census, etc.

**Survey:** Gathering data from the **sample** in order to make conclusions about the population.

For example, opinion polls, quality control checks in manufacturing units, etc.

#### **Parameter and Statistic**

Parameter: A descriptive measure of the population.

For example, population mean, population variance, population standard deviation, etc.

Statistic: A descriptive measure of the sample.

For example, sample mean, sample variance, sample standard deviation, etc.

# **Statistical Notations**

#### **Greek – Population Parameter**

Mean – μ Variance – σ<sup>2</sup> Standard Deviation - σ Roman – Sample Statistic Mean –  $\bar{x}$ Variance –  $s^2$ Standard Deviation - s

### Variables - Dependent and Independent

- Dependent variables on y-axis and Independent on x-axis.
- Dependent variable also called Target variable or Class
  Simple Linear Regression
  (with a continuous dependent [Y] variable)



# Variables



### Categorical Data (Qualitative)

#### Nominal Examples

- Employee ID
- Gender
- Religion
- Ethnicity
- Pin codes
- Place of birth
- Aadhaar numbers

Ordinal Examples

- Mutual fund risk ratings Fortune 50 rankings
- Movie ratings

While there is an order, difference between consecutive levels are not always equal.

#### **Discrete and Continuous**



#### **Discrete or Continuous?**

- Time between customer arrivals at a retail outlet Continuous
- Sampling 100 voters in an exit poll and determining how many voted for the winning candidate Discrete
- Lengths of newly designed automobiles -Continuous
- No. of customers arriving at a retail outlet during a five- minute period Discrete
- · No. of defects in a batch of 50 items
- Discrete

### Numerical or Categorical?

Age	Gender	Major	Units	Housing	GPA	
18	Male	Psychology	16	Dorm	3.6	
21	Male	Nursing	15	Parents	3.1	
20	Female	Business	16	Apartment	2.8	
<u> </u>						
	• Numeri	Categor	rical			
- Age			🗖 Gende			
- Units			🗖 Major			
- GPA			u Housi	ng		



- 1. Frequency Distribution
- 2. Bar Chart
- 3. Histogram

# Modality



# Symmetry



# **Central Tendency**



# Variability



# **Central Tendencies**

The reliable quantity

### Mean – Median - Mode

Mean, 
$$\mu = \frac{\Sigma x}{n}$$

Median: Arrange data in increasing order and find the mid-point  $\frac{(n+1)}{2}$ .

Mode – the most frequently occurring

# Player A vs Player B

Match	Player A	Player B
1	40	40
2	40	35
3	7	45
4	40	52
5	0	30
6	90	40
7	3	29
8	11	43
9	120	37
SUM	351	351
MEAN	39	39
MEDIAN	40	40
RANGE	120	23

### Who's Best?

Match	Player A	Player B
1	40	40
2	40	35
3	7	45
4	40	52
5	0	30
6	90	40
7	3	29
8	11	43
9	120	37
SUM	351	351
MEAN	39	39
MEDIAN	40	40
STANDARD DEVIATION	41.5180683558376	7.28010988928052

# Spread of Data

### **Measuring Variability and Spread**

Basketball coach Statson is in a dilemma choosing between 3 players all having the same average scores.

Points scored per game	7	8	9	10	11	12	13
Frequency, f	1	1	2	2	2	1	1

Points scored per game	7	9	10	11	13
Frequency, f	1	2	4	2	1

Points scored per game	3	6	7	10	11	13	30
Frequency, f	2	1	2	3	1	1	1

### **Measuring Variability and Spread**

Basketball coach Statson is in a dilemma choosing between 3 players all having the same average scores.

Points scored per game	7	8	9	10	11	12	13
Frequency, f	1	1	2	2	2	1	1

Points scored per game	7	9	10	11	13
Frequency, f	1	2	4	2	1

Points scored per game	3	6	7	10	11	13	30
Frequency, f	2	1	2	3	1	1	1

Mean = Median = Mode = 10 for all 3.



### **Measuring Variability and Spread**

#### Range = Max - Min

Points scored per game	7	8	9	10	11	12	13
Frequency, f	1	1	2	2	2	1	1

Points scored per game	7	9	10	11	13
Frequency, f	1	2	4	2	1

Points scored per game	3	6	7	10	11	13	30
Frequency, f	2	1	2	3	1	1	1

Points scored per game	7	8	9	10	11	12	13
Frequency, f	1	1	2	2	2	1	1

Points scored per game	7	9	10	11	13
Frequency, f	1	2	4	2	1

Points scored per game	3	6	7	10	11	13	30
Frequency, f	2	1	2	3	1	1	1

MEAN = MEDIAN = MODE = 10 RANGE = 5, 5, 27 Reject Player 3

### **SD** and Variance

### **Measuring Variability and Spread**

Variance =  $\frac{\Sigma(x-\mu)^2}{n} = \frac{\Sigma x^2}{n} - \mu^2$  (Derive) 3 3 6 7 7 10 10 10 11 13 30

Units are squared, which is not intuitive. Standard Deviation,  $\sigma = \sqrt{Variance}$ 

#### Basketball coach Statson is in a dilemma choosing between 3 players all having the same average scores.

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Points scored per game	7	9	10	11	13
Frequency, f	1	2	4	2	1

STANDARD DEVIATION

Player 1 = 1.7873008824606 Player 2 = 3.30823887354653

What is your Decision?????????

### **Data Visualization - Plots**

1. Box Plot

2. Scatter plot

3. Density Plot

# Box Plot



- Shows the data spread for individual

columns

### Scatter Plot

Ice Cream Sales vs Temperature						
Temperature °C	Ice Cream Sales					
14.2°	\$215					
16.4°	\$325					
11.9°	\$185					
15.2°	\$332					
18.5°	\$406					
22.1°	\$522					
19.4°	\$412					
25.1°	\$614					
23.4°	\$544					
18.1°	\$421					
22.6°	\$445					
17.2°	\$408					



#### - Shows relationship between 2 columns

#### Line of Best Fit



# Density Plot



- Shows the distribution of data

# Statistical simulation link

http://www.shodor.org/interactivate/activities/

# Percentile & Quartile

Nth percentile – States that there are atleast N% of values less than or equal to this value and (100-N) values are greater or equal to this value

i = (N/100)\*n

N – The percentile you are interested

n – Number of values

#### Key points

- 1. If i is decimal then round off to next value
- 2. If i is integer then take average of **i and i+1** value

# Let's calculate 85<sup>th</sup> percentile

#### Data:

3310 3355 3450 3480 3480 3490 3520 3540 3550 3650 3730 3925

Calculate 85<sup>th</sup> percentile ?

**Quartile** Dividing data into <sup>1</sup>/<sub>4</sub> – 4 parts

- Q1 First Quartile 25<sup>th</sup> percentile
- Q2 Second Quartile 50<sup>th</sup> percentile (Median)
- Q3 Third Quartile 75<sup>th</sup> percentile

IQR (Inter Quartile Range) = Q3 – Q1

# Case Study

In an Under 19 World Cup selection squad for 2018 the BCCI needs to select 1 player based on the current performance in 2017 – 2018 Ranji Trophy. There are 2 players with similar stats and the board is not sure whom to select

- Can you help the board members with your analysis ?

# Stats - Player X & Y

Runs scored by both players in last 14 matches

Player X		Player Y
	40	35
	20	40
	5	7
	20	23
	10	20
	75	26
	100	12
	25	30
	15	27
	15	102
	20	18
	17	17
	11	14
	5	7

# **Coefficient of Variation**

Calculate the descriptive statistics of both players and if the coefficient of variation is greater than 85% then drop that player

Coeff of Variation = (Standard deviation/ Mean) \* 100 %

# **Central Limit Theorem**

When samples of size n>=30 are drawn from a population and distributed with individual samples mean then any distribution changes to normal distribution



### **Key Points**

(Also called as Standard Error - SE) Standard deviation of sample mean = (population standard deviation/square root(n))

Mean of mean sample distribution = Population mean

As n increases SE decreases – SE is inversely proportional to n

# Measure of association between 2 variables

- 1. Covariance
- 2. Correlation coefficient

## Covariance

$$|Cov(X,Y) = \frac{\sum (X_i - \overline{X}) * (Y_i - \overline{Y})}{n}$$

#### Higher the value stronger the relation between them

# **Correlation coefficient**

$$r_{xy} = \frac{Cov(x, y)}{S_x \times S_y}$$

#### **Key Points**

1. A measure of relationship not affected by the units of measurements

2. Ranges from -1 to +1

# **Types of Correlation**

